

UNIVERSITY OF NAIROBI
DEPARTMENT OF MECHANICAL AND MANUFACTURING ENGINEERING
FME 211/212 – THEORY OF MACHINES LABORATORY EXPERIMENT

TITLE: Belt Friction

OBJECT:

To determine the coefficient of friction between belt and pulley and to check the effect of lap angle on the grip of the belt

APPARATUS:

See Fig. I. The belt friction rig consists of a pulley *A* free to rotate about the spindle *B*. The arm *C* can be adjusted to give various lap angles to the belt under test.

The belt *D* is connected to the spring balance *E* attached to the arm *C*. A weight carrier is hung on the other end of the belt, which hangs over the pulley wheel.

METHOD:

Arm *C* is set to the required Lap Angle and a weight added to the weight carrier (*T₂*). The pulley wheel is then twisted by hand in the direction that will increase the reading on the spring balance (*T₁*). The *static friction coefficient* can be determined from the value of (*T₁*) just before the *belt slips*. Further weights should be added to the carrier until the spring balance reads approximately 25 kgf. Weights should then be removed from the carrier so as to give 5-7 equally spaced readings between 0 and 25 kgf for *T₁*.

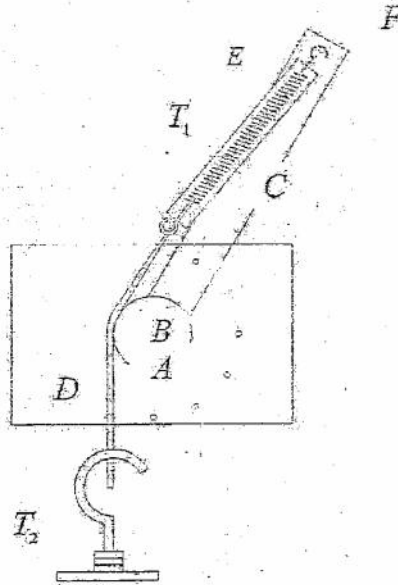


Figure I

(*For your calculations $1 \text{ kgf} = 4.45 \text{ N}$)

THEORY:

A flat belt is wrapped round a segment of a flat pulley. The limiting tensions in the two ends of the belt are T_1 and T_2

Refer Fig 3

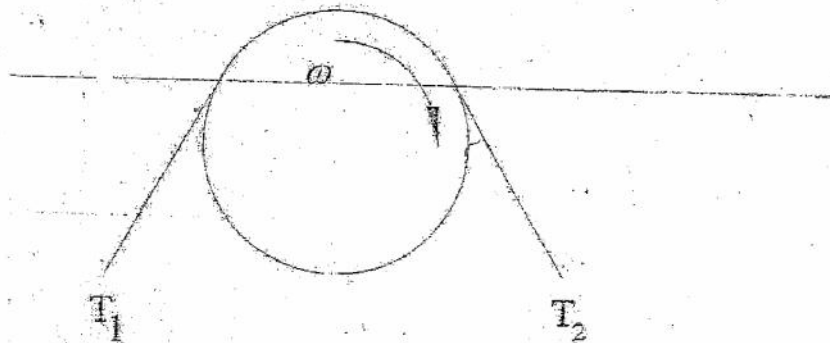


Figure 2.

Consider a small arc of the pulley θ . The tension on one side will be T and the other side $T + \theta T$.

Let the radial reaction C , the element of the belt be R . Then for the limiting case, the frictional force = R .

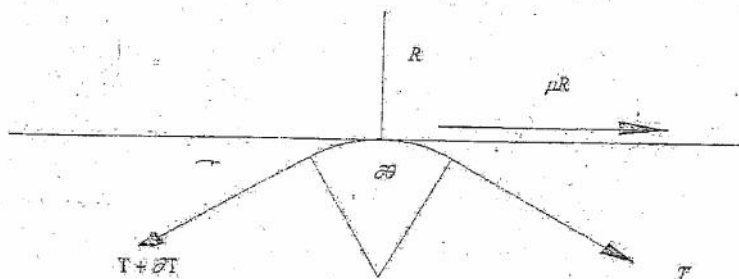


Figure 3

Resolving forces radially, $R = (T + \partial T) \sin \frac{\partial \theta}{2} + T \sin \frac{\partial \theta}{2}$

Neglecting 2nd order of small quantities, and writing $\sin \partial \theta = \partial \theta$, then

$$R = T \partial \theta \quad \dots (i)$$

Then resolving forces tangentially, $\partial T = R \quad \dots (ii)$

From (i) and (ii) $\partial T = T \partial \theta$

$$\text{Or } \frac{\partial T}{T} = \alpha \partial \theta$$

Integrating,

$$\int_{T_1}^{T_2} \frac{\alpha T}{T} = \mu \partial \theta$$

$$\text{i.e. } T_2 = T_1 e^{\mu \theta} \quad \dots (iii)$$

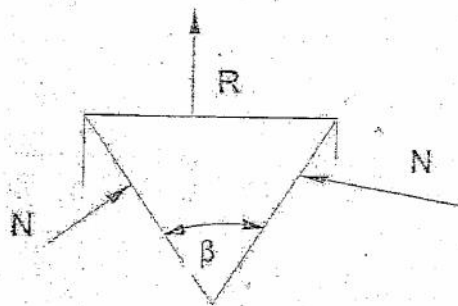


Figure 4

Note that this equation holds only when a slip is impending.

Refer to Fig IV above.

For a vee-belt the normal reaction between belt and pulley = N

$$\therefore R = 2N \operatorname{cosec} \left(\frac{\beta}{2} \right), \text{ where } \beta \text{ is vee or groove angle.}$$

Then for the limiting case,
Frictional force = $2\mu N$

$$\mu R \operatorname{cosec} \frac{\beta}{2} \dots\dots\dots (\text{iv})$$

$$\partial T = \mu R \operatorname{cosec} \left(\frac{\beta}{2} \right) \dots\dots (\text{v})$$

Equation (v), in conjunction with equation, (i) which still holds, finally yields, on integration

$$\frac{T_1}{T_2} = e^{\mu\beta} \operatorname{cosec} \frac{\beta}{2} \dots\dots (\text{v})$$

EXPERIMENTAL RESULTS

Graphs of T_1 against T_2 should be obtained for lap angles of 30, 90, 135 and 180 each curve consisting of 5-7 equally spaced points to give values of T_2 between 0-25 kgf.

From the best straight line of the points, the ratio $\frac{T_1}{T_2}$ is found, and the value for μ calculated.

CONCLUSIONS

Comment on the accuracy of your results and give your ideas as to why there should be any variation in the value of μ as found at the different lap angles,