

### EXPERIMENT ON FIXED BEAM

**Objective :** To perform deflection experiment on a beam fixed at both ends  
(Fixed Beam )

**Theory:** The expressions for the loadings (Point Loads) and the corresponding deflections for a fixed end beam are as indicated below for three cases namely:

**Case 1 :**

Fixed end beam loaded at the centre by a point load ( $W$ ) and the corresponding deflection ( $\delta$ ) measured at the centre of the beam. (See Fig1 below)

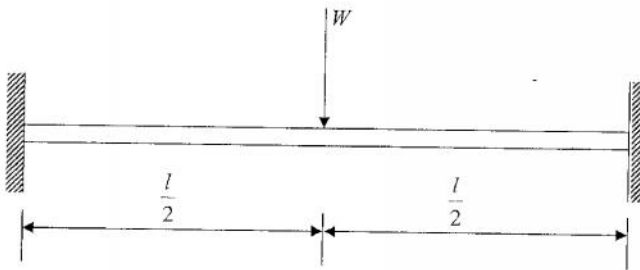


Fig 1

$$\delta = \frac{Wl^3}{192EI} \dots\dots\dots(1)$$

where  $E$  is the Modulus of Elasticity of the beam and  $I$  the Second Moment of Area of the cross-section about a horizontal axis through the centre of gravity.

**Case 2 :**

Fixed end beam loaded by a point load  $W$  located at a point distance ' $a$ ' from the left-hand end and distance ' $b$ ' from the right-hand end, with the corresponding deflection ' $\delta$ ' being measured at the point of application of the load.

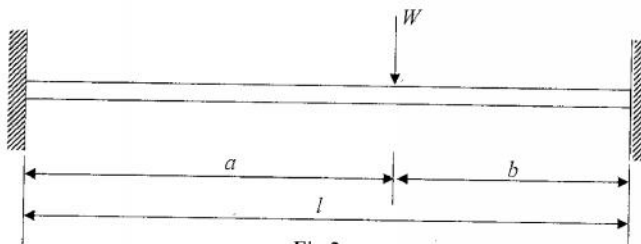
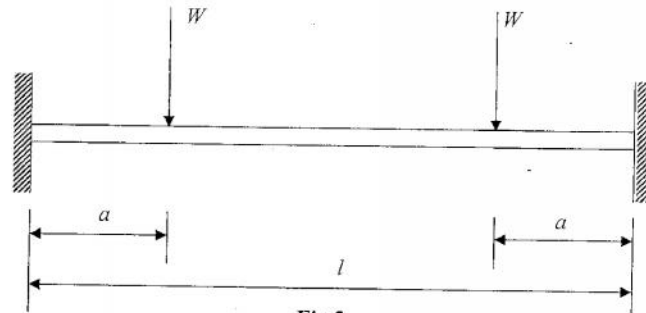


Fig 2

$$\delta = \frac{Wa^3b^3}{3l^3EI} \dots\dots\dots(2)$$

**Case 3 :**

Fixed -end beam supporting two equal point loads each of magnitude  $W$  and positioned at equal distances ' $a$ ' from each end with the deflection measured at the centre of the beam.



$$\delta = \frac{Wa^2}{24EI}(3l - 4a) \dots\dots\dots(3)$$

**Method :**

**Case 1 :**

For a given fixed -end beam, measure the cross-sectional dimensions of the beam using a vernier caliper and measure the length ' $l$ ' of the beam using a ruler. Apply an increasing point load ' $W$ ' at the centre of the beam and measure the corresponding deflection using a dial gauge mounted on a magnetic stand. From the series of readings obtained of the load ' $W$ ' against deflection ' $\delta$ ', draw a graph of the load ' $W$ ' against deflection ' $\delta$ '. From the slope ( $W/\delta$ ) of the graph obtained, calculate the value of the Modulus of Elasticity ( $E$ ) of the beam from the re-arranged equation 1 as indicated below:

$$E = \left(\frac{W}{\delta}\right) \frac{l^3}{192I} \dots\dots\dots(4)$$

**Case 2 :**

For a given fixed -end beam, establish the distance ' $a$ ' and distance ' $b$ ' along the Length of the beam. Apply an increasing point load ' $W$ ' ( at a point distance ' $a$ ' From the left-hand support ) and measure the corresponding deflection using a dial

Indicator mounted on a magnetic stand. From a series of readings obtained of the load 'W' and the corresponding deflection 'δ', draw a graph of the load 'W' against deflection 'δ'. From the slope  $\left(\frac{W}{\delta}\right)$  of the graph obtained, calculate the value of the Modulus of Elasticity (E) of the beam from the re-arranged equation 2 as indicated below :

$$E = \left(\frac{W}{\delta}\right) \frac{a^3 b^3}{3l^3 I} \dots\dots\dots(5)$$

**Case 3 :**

For a given fixed-end beam , establish the distance 'a' from the end. Apply increasing two equal loads W ( at points 'a' from each end ) and measure the corresponding deflection 'δ' at the centre of the beam using a dial indicator mounted on a magnetic stand. From a series of readings obtained of the two equal loads 'W' and the corresponding deflection 'δ', draw a graph of the load 'W' against deflection 'δ'. From the slope  $\left(\frac{W}{\delta}\right)$  of the graph obtained, calculate the value of the Modulus of Elasticity (E) of the beam from the re-arranged equation 3 as indicated below:

$$E = \left(\frac{W}{\delta}\right) \frac{a^2 (3l - 4a)}{24I} \dots\dots\dots(6)$$

**Discussion :**

Discuss the results obtained